Hybrid Swarm Intelligence Algorithm for Solving Vehicle Routing Problem with Time Windows

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ABSTRACT

Vehicle Routing Problem is formulated to tackle the issues related to distributing fuel to delivery stations, in certain cases, the client shall specify a period-window for the delivery and this comes under the class of vehicle routing problem with time windows. The vehicle routing issue considered in this paper is the dynamic VRPTW with Solomon's data sets. The target is to find the minimum number of vehicles and distance travelled based on hybrid swarm intelligence algorithm. The proposed methodology hybridized the exploration and exploitation ability of the Multi Verse Optimization Algorithm (MVO) and the Ant Lion Optimizer (ALO) algorithm. The performance of the proposed hybrid optimization algorithm is analyzed with respect to the number of vehicles, distance travelled, and computational time for all the developed techniques and to validate the proposed models. Assessed results registered utilizing the proposed hMVO-GHO technique is compared with the available techniques of literature for solving the Solomon VRPTW problem to illustrate the effectiveness of the proposed hMVO-GHO algorithm.

Keywords:

Vehicle Routing Problem, VRPTW, Solomon's data set, hybrid MVO-GHO

1.Introduction

The optimal route selection for specific number of vehicles that are scheduled to serve the customers who are available in certain time windows is a serious problem of concern. The ultimate aim of the problem is to reduce the transportation cost by reducing the travelling distance with constrain of all the customers should be visited only once, such problem is termed as vehicle routing problem with time window. One of the important combinatorial optimization problems is the VRPTW and is a notable problem in transportation problems. VRPTW is more towards finding the optimal routes for the movement of identical vehicles with limited capacity and as well that gets departed from a central yard and function for different customers who are geographically located with pre-set time windows and of known demands. The vehicles return to the central yard (depot) at a specified time window and with an optimal route. In this process, each customer is visited only once by one vehicle with respect to the specified time window (Moradi 2019). The time window definition will be based on the initial and final time for beginning the service. VRPTW problems are widely employed in real-time scenarios of food delivery, postal services, waste material accumulation, college and school bus routing, Delivery of cash at bank and ATM points and several other maintenance operations. In large-scale VRPTW, a multi-objective optimization problem is one of the difficult problems wherein the exact techniques fail to find required solutions because of the run time parameter. The key objectives to be determined in this multi-objective combinatorial optimization problem is,

- Minimization of the number of vehicles in the routing path
- Minimization of total distance travelled employing a minimal number of vehicles.



Figure. 1A simple VRPTW

Figure 1 shows a simple VRPTW, the central yard of location is specified by 'Z' and the customers are represented from 1 to 12. The Figure shows four routes and their four solution routes are given by Z-6-1-4-Z, Z-3-11-9-5-Z, Z-7-10-12-Z, and Z-2-8-Z. Considering the complexity and applicability, exhaustive research work has been carried out employing scrupulous and approximate techniques which include heuristic and meta-heuristic algorithms to solve VRPTW. Approximate reasoning techniques are capable of determining optimal/ near-optimal solutions for these multi-objective VRPTW instances incurring minimal run time. VRPTW being a constrained multi-objective optimization problem belong to the non-deterministic polynomial hard problem and henceforth are the stochastic population-based evolutionary optimization techniques and swarm intelligent approaches which can provide suitable solutions to these problems. Thus, in this proposed work, the focus is done on the development of hybrid multi-verse optimizer to attain near-optimal solution to this multi-objective VRPTW.

2. Existing Works of Literature

To solve the multi-depot green optimization algorithm (MDVRP) a modified anlt colony optimization algorithm is developed by Li et al. (2019). Stodola (2020) introduced probabilistic techniques with state- of art methods to solve MVDRP. On considering the flexible timing windows the vehicle routing problem is solved by a hybrid ant colony optimization algorithm, Zheng et al. (2019). An evolutionary optimization algorithm is developed to solve VRPTW based on combining the features of evolutionary scatter optimizer and PSO strategy, the association between the total vehicle traveled and the total distance is employed to identify the search direction. Mendoza et al. (2020) employed a hybrid grasshopper optimization algorithm to solve the VRP to identify the optimal routes. Alinaghian & Shokouhi (2018) discussed on routing problem with constrain where the split delivery cannot be accepted and only one vehicle should be employed to deliver the products. PSO is employed to optimize the capacitated vehicle routing

problem, the total waste collection efficiency, fuel efficiency, the total cost is employed as problem constraints(Hannan et al. 2018). Goel & Maini (2018) incorporated a firefly optimization strategy with Ant colony algorithm to solve the routing problem. Sedighizadeh & Mazaheripour (2018). The PSO and ACO is combined to present a hybrid strategy that is employed to solve the routing problem. Dewi & Utama (2021) proposed a hybrid WOA optimizer on combining the characteristics of WOA and the Tabu search optimization algorithm. Sitek et al. (2021) applied a hybrid approach to solve a CVRP with alternative pic-up delivery and time windows. Pan et al. (2021) studied a Duration Minimizing VRP with timing window by employing an adaptive large neighborhood search and Tabu algorithm. Euchi, and Sadok (2021) proposed a hybrid GA for VRP that utilizing a drones. An effective model for Vehicle routing problem was proposed by Moradi (2019) with timing window by a novel interrogative way, the performance has tested with benchmarks. A multi-adaptive model which concerns three adaptive strategies of vehicle directing issue with timing window, which uses (PSO algorithm) particle swarm optimization and the model has tested with two datasets that includes 56 and 300 instances, also compared with some other PSO versions by Marinakis et al. (2019). The model with CLP- Constraint Logic Programming and MP Mathematical Programming was introduced by Sitek & Wikarek (2019) for handling the delivery of postal, place of dispatch, and the timing window that is delivery time. Performance of the model has improved by introducing heuristic in the place of MP. The same issues with multi-commodity network are considered by Yang et al. (2020) using Lagrangian relaxation formula. A Multi Objective model with SA - Simulate Annealing and IACO - Improved Ant Colony Optimization was introduced by Wang et al. (2020) to handle the service choice problem and timing window problem. The model has been tested using solomon's and Cordeau's benchmarks. By considering the minimized travelling time and various vehicles from various depots Zhen et al (2020) propose a model with release date and timing window. This model uses hybrid PSO and Genetic Algorithm with the improved efficiency. Shen et al. (2020) introduced a model to reduce the total travelling distance by considering the timing window. The model has designed by hybridizing BSO (Brain Storm Optimization) and ACS (Ant Colony System). Along with the distance reduced cost and the time in health care been introduced by the model proposed by Euchi et al.(2020) using artificial The survey demonstrates the implementation of various swarm intelligence techniques. intelligence algorithms for solving of VRPTW. Nevertheless, specific problems cannot be solved in an efficient way employing a single one technique since each of them possesses its own merits and demerits. These observed limitations are the driving power behind the development of hybrid optimization techniques. When two or more techniques are combined, the merits of the individual algorithms are brought out and tend to provide more effective solutions for complex problems. Based on the utility of these algorithms and considering the no free lunch theorem, there is always a need for the development and hybridization of the optimization algorithms. The main reason behind the development of hybrid MVO-GHO technique includes,

- Parallel and redundant mechanism of these two algorithms is brought out.
- Designed to be fault- tolerant as they apply intensive computation
- Improves both the exploration and exploitation process
- Both these algorithms are gradient-free and moves towards attaining better solutions in the broader search space.
- MVO and GHO tend to be co-operative with each other
- Continuous adaptation of the algorithms
- .

3 Problem Statements

The VRPTW is defined as follows: There exist 'n' customers who are about to be served and each of these customers need a product or services to be done. A convoy of indistinguishable vehicles is located in the central yard for rendering service to the customers. The volume and capacity of every vehicle should be greater than or equal to the sum of all the demands on the traversed route by the vehicles. Each customer has to be compulsorily served only once and only by one vehicle within the specified time window. The time window will be based on the pre-set time interval indicated by the initial and final arrival time. The vehicles have to reach the customer place before the final time of arrival. A vehicle may be permitted to reach before the initial arrival time, wherein in this case, it has to wait until the initial arrival time and then tends to provide service to the customer. Every customer authorizes an additional assistance time to the course for stacking or emptying the items or dependent on an opportunity to convey the items or perform different administrations. Each vehicle has to leave from the customer place and go back to the central yard (depot) within a particular time window. For the VRPTW problem, the solution will be the set of routes wherein the vehicle begins from the central yard, meets the customer services, and comes back to the initial start point concerning the capacity and indicate time window constraints. The number of routes on the network is equal to the size of the convoy and a single vehicle will be dedicated to a single route.

VRPTW, a multi-objective optimization problem comprises minimizing the number of vehicles to be used (convoy size) and the total distance that is covered by the vehicles for meeting the required demands of the customers. The mathematical foundation of VRPTW is as given below: There exists a non-directed complete graph CG = (N, Y), with $N = \{n_0, n_1, n_2, ..., n_n\}$ and $Y = \{(n_i, n_j) | n_i, n_j \in N, i \neq j\}$ represents the node-set and the arc set. The given ' n_0 ' indicates the central yard point and n_i (i = 1, 2, 3, ..., n) specifies the customers. The customers get serviced from the convoy of identical vehicles using the same volume capacity 'V'. Each node is linked with a demand quantity v_i and indicated via a time window $[y_i, t_i]$, here the node n_0 gets associated with $v_0=0$ and $[0, t_0]$.

In respect to the time window constraint, a vehicle 'p' has to come to the customer 'i' location t_i^p before the final arrival time f_i . Also, moving before the initial arrival time a_i comes across waiting time w_i . Every customer 'i' possess a serving time s_i , and it is the original time the delivery takes when the vehicle has arrived at the customer point. Every vehicle has to complete its route within the specified time window given by the central yard. Every arc present in the network indicates a connection that exists between two nodes along with a travelling distance TD_{ij} , which is the Euclidean distance among the nodes n_i and n_j , and a travelling time TT_{ij} , that is proportional to the travelling distance. Let 'N' specify the number of customers and the 'S' indicates the number of vehicles or the convoy size, then the optimization model of the VRPTW is defined as given below.

$$\begin{cases} \min F(x) = (f_1, f_2) \text{ with} \\ f_1 = S \\ f_2 = \sum_{i=1}^N \sum_{j=0, j \neq i}^N \sum_{p=1}^P TD_{ij} x_{ij}^p \end{cases}$$
(1)

Where, the functions ' f_1 ' and ' f_2 ' are the two objective functions to be minimized in this NP-Hard combinatorial optimization problem subject to the constraints,

$$\sum_{j=1}^{N} x_{0j}^{p} = \sum_{i=1}^{N} x_{i0}^{p} = 1, \ p \in \{1, 2, 3, ..., P\}$$
(2)

$$\sum_{j=0, j\neq i}^{N} x_{ij}^{p} = \sum_{\substack{j=0, j\neq i\\ \in\{1,2,3,\dots,P\}}}^{N} x_{ji}^{k} \le 1, i \in \{1,2,3,\dots,N\}, p$$
(3)

$$\sum_{p=1}^{P} \sum_{i=0, i\neq j}^{N} x_{ij}^{p} = 1, \ j \in \{1, 2, .3, ..., N\}$$
(4)

$$\sum_{p=1}^{P} \sum_{j=0, j\neq i}^{N} x_{ij}^{p} = 1, i \in \{1, 2, .3, ..., N\}$$
(5)

$$\sum_{i=0}^{N} q_{i} \sum_{j=0, j \neq i}^{N} x_{ij}^{p} \leq V, \ p \in \{1, 2, .3, ..., P\}$$

$$t_{i}^{p} + w_{i}^{p} + s_{i} + t_{i} = t_{i}^{p} \ i \ i \in \{1, 2, 3, ..., P\}$$

$$i \neq i, \ p \in \{1, 2, .3, ..., P\}$$

$$(6)$$

$$v_{i} \leq \left(t_{i}^{p} + w_{i}^{p}\right) \leq t_{i}, i \in \{0, 1, 2, 3, ..., N\}, p \in \{1, 2, ..., S\}$$

$$(7)$$

In the above,

$$x_{ij}^{p} = \begin{cases} 1 & \text{when vehicle ' } p' \text{ travels from } v_{i} \text{ to } v_{j} \\ 0 & \text{otherwise} \end{cases}$$
(8)

Equation (1) specifies the two objective (fitness) functions f_1 and f_2 to be minimized indicating the number of vehicles employed and the total distance traversed respectively. Equations (2) and (3) give the constraints that guarantee the vehicles initiate the delivery process from the central yard and provide service to customers individually one by one and then finally comes back to the central yard. The constraints provided in the Equations (4) and (5) represents that a customer is traversed only once and by only one vehicle. The constraint in equation (6) indicates the number of services or the products delivered by each vehicle that cannot exceeds its capacity V. Equation (7) indicates the computation of the travel time and the existence of time windows. Equation (8) represents that x_{ij}^p is equal to 1 when vehicle 'p' moves from node n_i to node n_j , and becomes equal to '0' otherwise. The ultimate aim is to solve this NP-Hard combinatorial VRPTW by the proposed hybrid optimization algorithm in order to achieve the best optimal route with all the specified constraints given in equations (2) to (8) and to minimize the objective function given in equation (1).

4. Proposed Methodology

In this article a novel hybrid strategy is developed on combining the best characteristics of Multi-Verse Optimizer and the Grasshopper Optimization algorithm (hMVO-GHO). The Multi-verse optimizer is viewed as an effective strategy for its exploration mechanism and it suffers to handle the poor exploitation ability, so in order improve its exploitation ability the grasshopper optimization technique is hybridized with it. The combined version of MVO with Grasshopper Optimization (GHO) moves towards the optimal solutions for VRPTW by exploring and exploiting the search space. The modified hybrid MVO-GHO technique is applied for the VRP with small-time windows and large time windows for Solomon problem instances and the fitness function minimization is carried out.

4.1 Multiverse Optimization Algorithm – An Overview

The concept of cosmology is inspired to develop a Multi-verse optimizer algorithm, Mirjalili et al. (2016). The multi-verse concept is contradictory to the concept of the universe and this specifies the presence of other universes along with the universe we are living in. The theory that multiple universes get interacted with each other through the white holes, black holes, and wormholes and as well get collided among themselves is the foundation of multi-verse theory. In MVO modelling, for exploring the search space white holes and black holes are used and for exploiting the search space wormholes are being employed. MVO optimization procedure is initiated by creating a population of distinct solutions and attempts to determine solutions based on the defined number of iterations. The update mechanism is done in MVO based on one of the theories of the potential existence of the multiple universes. Hence, a single universe represents an optimization solution and each object in the universe corresponds to the decision variable about the problem. The elements of the Universe is presented in Figure 2 and the operation of MVO is based on the following factors,

- Higher probability of white holes occurs with a higher inflation rate
- Lower probability of black hole specifies higher inflation rate
- The transfer of objects in the universe takes place from a white hole into a black hole
- Considering all universes, the objects tend to move towards the best universe



(a)White hole

(b) Worm hole

(c) Black hole

Figure 2 Elements of Multiverse optimizer

Black holes with lower expansion rates get the items from the white holes with a higher swelling rate. Through the iterative process, the mean inflation rate is improved and the universes gets arranged to their inflation rates during each iteration and the white hole gets assigned to the universe using roulette wheel selection. The matrix that defines the population is given by,

$$U_{pop} = \begin{bmatrix} x_{1} & \dots & x_{1}^{d} \\ x_{2} & \dots & x_{2}^{d} \\ \dots & \dots & \dots \\ x_{n} & \dots & x_{n}^{d} \end{bmatrix}$$
(9)

In Equation (9), the variable ' U_{pop} ' represents the universes called population, 'n' is the number of universes and the number of dimensions is indicated by 'd'. The decision variable is generated using,

$$x_i^j = \left\{ low_bd_j + rand() \left((upr_bd_j - low_bd_j) + 1 \right)$$
(10)

with i=1,2,..n and j=1,2,...d, the lower bound and upper bound specifies the bound limit of the decision variable and rand() generates a random number from 0 to 1. During the iterative

process, the decision variable that possesses a black hole changes its value employing two choices as given by,

$$x_{i}^{j} = \begin{cases} x_{np}^{j} & rand I() < Norm(UV_{i}) \\ x_{i}^{j} & rand I() \ge Norm(UV_{i}) \end{cases}$$
(11)

Where, ' x_i^j ' indicates the j-th decision variable of the i-th universe, 'UVi' specifies the ith universe, ' $Norm(UV_i)$ ' represents the normalized inflation rate in respect of the i-th universe, 'rand1()' is a randomly generated number between [0,1] and ' x_{np}^j ' represents the j-th variable of m-th universe, that is selected here using Roulette Wheel. The diversity of the solutions has to be increased and this is carried out with the wormhole and the algorithm progresses assuming that wormholes exist in the solution randomly. This is given by,

$$x_{i}^{j} = \begin{cases} x_{fit_{j}} + \eta \times ((upr_{bd_{j}} - low_{bd_{j}}) \times rI + low_{bd_{j}}) & r2 < 0.5 \\ x_{fit_{j}} + \eta \times ((upr_{bd_{j}} - low_{bd_{j}}) \times rI + low_{bd_{j}}) & r2 \ge 0.5 \\ x_{i}^{j} & r3 \ge P_{wh} \end{cases}$$
(12)

In Equation (12), ' x_{fit_j} represents j-th fittest universe variable that has been generated as of then, the minimum bound limit and maximum bound limit of j-th parameter is given by low_bdj and upr_bdj respectively with x_i^j indicating the j-th parameter of the i-th universe, r1, r2 and r3 are random numbers from 0 to 1, ' η ' is the rate of distance travelled and ' P_{wh} ' indicates the probability of the presence of wormholes. The adaptive variation of the parameters ' η ' and ' P_{wh} ' are given by,

$$\eta = 1 - \frac{(current_iteration)^{1/ea}}{(max_iteration)^{1/ea}}$$
(13)
$$P_{wh} = C_{min} + current_iteration \times \left(\frac{C_{max} - C_{min}}{max_iteration}\right)$$
(14)

Where, '*ea*' represents the exploitation accuracy during the iterative process, '*Cmin*' and '*Cmax*' indicate the predefined constant values which help for the exploitation phase during iterations. Higher the value of '*ea*', more accurate and faster is the exploitation mechanism. The procedural steps adopted during the algorithmic process of MVO are presented below:

Step 1: Initialize the necessary parameters

Step 2: Generate the solution set of the individuals

Step 3: Compute the fitness function for all the generated solution sets

Step 4: Based on the computed fitness function, arrange the solution sets in the order of best to worst.

Step 5: Update each solution based on the white/black holes and wormholes

For considered 'j'-th decision variable of solution (x_i)

Generate random value *rand1()* and compare it with the objective function value xi and exchange it with 'j'

Case 1 – The value gets replaced with better solutions

Case 2 – The value remains the same

Generate random value 'r2' to compare with the probability of wormhole existence ' P_{wh} ' and exchange it with 'i',

Case 1 – The value gets replaced from the best solution after adding ' η ' value.

Case 2 – The value gets replaced from the best solution after Subtracting ' η ' value.

Perform steps 3 to 5 repeatedly until the required end fitness value is achieved. Step 6: Return the best solution evaluated during the iterative process.

4.2 Grasshopper Optimization Algorithm – An Overview

The Grasshopper Optimizer is a swarm intelligence algorithm developed based on inspiring the social behaviour of grasshoppers, they are capable of migrating over large distances and during their traversal path they consume vegetation and once they move to adulthood, they tend to swarm in the air. The key feature of the swarm is a slow movement in the larval stage and small steps of grasshoppers but in contradictory the adulthood feature is abrupt movements and large steps. One of the significant qualities of amassing of grasshoppers is the mode wherein they reach and look for the food. This is done by grasshoppers using the exploration and exploitation process; at the exploration phase the search agents are motivated to move abruptly and at the exploitation phase they move locally. The exploration and exploitation mechanism and that of the identifying and seeking the target food source is carried out by grasshopper naturally. The life cycle of grasshopper is presented in Figure 3.





Figure 3 Grasshopper life cycle

The swarming behaviour of grasshopper is represented by the mathematical equation, $X_i = S_i + G_i + A_i$ with random behaviour included, (15)

 $X_i = r_1 S_i + r_2 G_i + r_3 A_i$ where $r_1, r_2, r_3 \in [0,1]$

In Equation (15), ' X_i ' denotes the i-th grasshopper position, ' S_i ' the social interaction, ' G_i ' the gravity force exerted on the grasshopper, and ' A_i ' denotes the wind advection. The entities social interaction, gravity force, and wind advection are given by,

$$S_{i} = \sum_{\substack{j=1\\j\neq i}}^{N} s(d_{ij}) \hat{d}_{ij} \text{ with } s - function as, s(p) = fe^{-\frac{p}{al}} - e^{-p}$$

$$G_{i} = -C_{g} \hat{e}_{g}$$

$$A_{i} = d_{u} \hat{e}_{w}$$
(16)

Where ' d_{ij} '- the distance between the 'i'-th and 'j'-th grasshopper, ' $d_{ij}=|x_j-x_i|$ ', 's' - the capability of societal group forces, 'f' is the intensity of attraction, 'al' - attractive length scale, ' C_g '- gravitational constant, ' \hat{e}_g '- Unity vector towards the center of the earth. ' d_u ' - drift constant,'

 \hat{e}_{w} '- Unity vector towards the wind direction, 'N' – Number of grasshoppers. Equation (16) in equation (15) becomes,

$$X_{i} = r_{I} \sum_{\substack{j=1\\j\neq i}}^{N} s(d_{ij}) \hat{d}_{ij} - r_{2}C_{g} \hat{e}_{g} + r_{3}d_{u} \hat{e}_{w} \quad where \quad r_{I}, r_{2}, r_{3} \in [0, 1]$$
(17)

In general, grasshoppers tend to reach the comfort zone and the swarm does not converge to a specified point. Considering this the equation (17) is modified as,

$$X_{i} = c \left(\sum_{\substack{j=l\\j\neq i}}^{N} c \frac{up_bd-lw_bd}{2} s \left(\left| x_{j}^{d} - x_{i}^{d} \right| \right) \frac{x_{j} - x_{i}}{d_{ij}} \right) + \hat{O}_{targ\,et}$$
(18)

Where, 'up_bd' represents the upper bound in the specified d-th dimension, 'lw_bd' is the lower bound in the specified d-th dimension, 'c' is the constant that diminish comfort, repulsive and attractive force, ' \hat{O}_{target} ' is the target along the direction of wind.

To adjust the exploration and exploitation course, the diminishing coefficient 'c' must be reduced relatively to the quantity of iteration. This coefficient is given by,

$$c = max_c - current_iteration \times \frac{max_c - min_c}{max_iterations}$$
(19)

Where, 'max_c' is the maximum value and 'min_c' specifies the minimum value. The value of 'max_c' is chosen as 1 and that of 'min_c' is chosen as 10^{-5} .

4.3 Proposed hybrid MVO-GHO optimization algorithm (hMVO-GHO)

A single optimization algorithm suffers to handle specific problem statement such as local stagnation issue, delayed convergence, pre-mature convergence and so on. These observed limitations are the driving power behind the development of hybrid optimization techniques. When two or more techniques are combined, the merits of the individual algorithms are brought out and tend to provide more effective solutions for complex problems. To attain better exploration and exploitation ability the exploitation mechanism of GHO is combined with the exploration mechanism of MVO, the hybrid MVO-GHO algorithm is developed. Initially the model is set to find the optimal solutions by MVO strategy, the fittest population generated from MVO is employed as search population for GHO, the pseudo code is presented in Algorithm 1. The modeled hybrid multi-verse optimizer - grasshopper optimization technique is enforced for Solomon benchmark data sets for VRPTW for demonstrating the effectiveness of the proposed algorithm. During the iterative process, the fitness functions, quantity of vehicles and absolute distance voyaged are assessed and the algorithm is roused to limit these fitness values. Employing a modified hybrid MVO-GHO technique, for selection of the decision variable from the universe Roulette wheel selection was employed and the exploration mechanism was carried out. At the time of iteration, the object updates are carried out with the white/black holes and wormholes. The classic grasshopper optimization algorithm gets invoked on attaining the first global best from the multi-verse optimization technique and it goes on with its swarming behaviour to perform position updates to attain a more effective solution. The hybrid operation of multi-verse optimizer and grasshopper optimization has resulted in achieving a balance between the exploration and exploitation mechanism due to both of its swarming nature and conditional movements inside the search space in reaching solutions. The hybrid mechanism makes the algorithm move towards solution set without getting stuck with local and global optima

problems, premature convergence, and attains faster convergence with better minimized fittest individuals in respect of the number of vehicles and total distance travelled.

Algorithm -1

//Modified hybrid MVO-GHO algorithm//
Initialize MVO-GHO parameters:
low_bd, upr_bd, number of universes, number of dimensions,
convergence criterion, ea, C _{max} , C _{min} , max_c, min_c and other random constants
Randomly generate the swarm of population
while (convergence_criterion) not met do
for all solution_set generated do
Compute the fitness function
Sort the solutions from the best one to worst one based on fitness value
Perform normalization of solution set - Norm (UV_i)
Update the best solution set $(x_{best i})$
for each solutions 'i' except the best solution set perform
Evaluate P_{wh} and n using equations (5) and (6)
Index blackhole = i
for each object x_i do
rand1=random(0.1)
<i>if</i> (rand1 <norm(uv<sub>i)) Then</norm(uv<sub>
Index whitehole=RouletteWheel selection
S(Index blackhole, j)=Sort(Index whitehole, j)
end if
r3=random(0,1)
if $(r3 < P_{wh})$ then
r2=random(0,1)
r1 = random(0, 1)
<i>if</i> $(r2 < 0.5)$ <i>then</i>
Update the position of solution_universe with
equation $(\hat{4}) - case \hat{1}$
else
Update the position of solution_universe with
equation (4) – case 2
end if
end if
end for
end for
Invoke GHO
$T=globalbest_solution (MVO)$
Update c
for each search agent
Normalize(Grasshoppers_Distance)
Update grasshopper_position using equation (18) for current search agent
<i>if</i> (boundary_exceeded)
best_agent=current_agent
else

update c and proceed further end if end for Update T (better_solution) Iteration=iteration+1 end for end while Return the best optimal solution T

The developed hybrid MVO-GHO is applied for the standard benchmark functions and its suitability in solving the NP-Hard combinatorial optimization problem is analyzed. The standard benchmark test functions for which the modified hybrid MVO-GHO applied are the same as given in Table 1.

Function	Function definition	Dimension	Range
De Jong first	$f(\mathbf{r}) = \sum_{n=1}^{d} \mathbf{r}^2$	50	[-5.12,5.12]
function	$J(x) - \sum_{i=I} x_i$		
Rosen brock	$f(r) = \int_{-\infty}^{d-1} \left[(1 - r)^2 + 100 (r - r^2)^2 \right]$	50	[-
test function	$J(x) = \sum_{i=1}^{2} \left[(1 - x_i) + 100(x_{i+1} - x_i) \right]$		2.084,2.084]
Schwefel	$f(\mathbf{r}) = \sum_{n=1}^{d} \left[-\mathbf{r} \sin\left(\sqrt{ \mathbf{r} } \right) \right]$	50	[-500, 500]
function	$J(x) = \sum_{i=l} [x_i \operatorname{Sin}(y x_i])]$		
Ackley	$(1) 20 \left[\begin{array}{c} 0 \\ 0 \\ 2 \end{array} \right] \left[\begin{array}{c} 1 \\ \frac{d}{2} \\ 0 \\ 2 \end{array} \right]$	50	[-32.768,
function	$f(x) = -20 \exp\left[-0.2\sqrt{\frac{\sum x_i}{d_{i=1}}}\right] - \exp\left[-\sum \cos(2\pi x_i)\right]$		32.768]
	+(20+e)		
	. ,		
Rastrigin	$f(x) = 10d + \sum_{n=1}^{d} \left[x^2 - 10 \cos(2\pi x) \right]$	50	[-5.12,5.12]
function	$J(x) = I0a + \sum_{i=1}^{n} [x_i - I0\cos(2\pi x_i)]$		

Table 1 Bench mark functions

The required parameters for the run of the hMVO-GHO algorithm are initialized and the iterative optimization process is carried out. The proposed modified hybrid MVO-GHO is applied for the considered five test functions with their dimensions to be 50. The comparison of the developed algorithms was done with the existing PSO, MVO and chaotic MVO (CMVO). Table 2 provides the results attained in applying the proposed optimization technique on the test functions. For the considered five test functions with a dimension of 50, it has to be noted that using proposed hMVO-GHO, the minimum, maximum and average values are minimal than that of the PSO, MVO and CMVO (Kennedy 1955, Mirjalili et al. 2016, Ewees et al. 2019). The proposed hybrid algorithm outperforms the conventional state of art methods such as PSO and MVO which confirms the applicability of the proposed hybrid MVO-GHO more suitable for the VRPTW problem.

 Table 2Test Function Results of Existing and Proposed Techniques

Functions	Dimension	Considered	Convergence	Minimum	Maximum	Average
		Algorithm	rate	value	value	value
De Jong	50	PSO	0.78	126	172	155
first		MVO	0.85	96	120	102

function		Chaotic MVO	1	114	136	122
		hMVO-	1	60	82	71
		GHO				
Rosen	50	PSO	1	167	192	175
brock		MVO	1	112	146	128
function		Chaotic	0.94	132	187	159
		MVO				
		hMVO-	1	48	70	59
		GHO				
Schwefel	50	PSO	0.72	146	165	151
test		MVO	0.89	124	147	133
function		Chaotic	1	138	156	143
		MVO				
		hMVO-	1	36	57	45
		GHO				
Ackley	50	PSO	0.92	189	202	195
function		MVO	0.81	153	180	167
		Chaotic	0.77	176	194	182
		MVO				
		hMVO-	1	40	61	49
		GHO				
Rastrigin	50	PSO	0.85	96	120	108
function		MVO	0.93	73	90	81
		Chaotic	0.77	55	70	64
		MVO				
		hMVO-	1	38	54	46
		GHO				

4.4 Experimental Analysis of the proposed Vehicle

The proposed techniques were implemented in MATLAB R2018b version and run on an Intel Core i5-7200U CPU @2.50GHz, 2712 MHz, 2 Core(s) and 4 Logical Processor(s) and 8 GB RAM. The parameter settings are given in Table 3 and these parameters were set with off-line tuning methods. To evaluate the model experimentally the Solomon's benchmark dataset that comprising of 56 sets is utilized (Solomon et al.1986, Solomon et al.1987, Solomon& Desrosiers 1988). The entire dataset is segregated into six classes such as R1, R2, S1, S2, SR1 and SR2 on considering the issues of the routing problem such as armada measure, vehicle limit, voyaging time of vehicles, spatial and worldly circulation of clients. The issues are assemblage in a class, for instance the issues in R class the customers are grouped time arrangement and S class possess sets on the basis of their location. The SR class consist of the attributes from both S class and R class. The class R1, S1 and SR1 possess the issues like the tight time arrangement for the terminal, consequently, a vehicle can serve only two clients. The other classes possess the set that are related to the case of more clients can be served by a vehicle with vast time deal. S2 and R2 allows customers to enjoy long booking skyline and large number of customers can be allotted for a single vehicle, so here the customer direction related issues are arranged in this class. On

accounting to the width of time arrangements the issues are flagged as 25, 50, 75 and 100 agreement.

Algorithmic parameters	Parametric values
Population size	150
Trial runs	30
P _{wh} (minimum)	0.2
P _{wh} (maximum)	1.0
Exploitation accuracy (ea)	6.0
T ₀	36
Convergence criterion	10 ⁻⁶
Maximum iterations	200
Selection	Boltzmann selection

Table 3 Parameter setting of the proposed hybrid algorithm

To validate the performance of the proposed hybrid MVO-GHO technique, the developed algorithms are applied over the 56 Solomon problem instances with 100 customers each. The developed hybrid optimization technique is simulated for the considered problem instances and the fitness functions – the number of vehicles and total distance travelled are minimized for the VRPTW. The algorithm hMVO-GHO is run for 30 trial runs and the best fitness values evaluated based on the object update in the universes are the required optimal solution set. The optimization iterative process is run until the convergence criterion is met and the evaluated solution sets are provided in Table 3 and Table 4 for the considered Solomon problem instances with small-time windows and large time windows respectively. The fitness function is given in Equation (1) is attained includes the number of vehicles (NV) and the Total Distance travelled (TD) for each of the vehicle routes taken. The evaluated number of vehicles and total distance travelled pertaining to the best optimal solution of the trial runs using hMVO-GHO is provided in Table 4 and Table 5 for the VRPTWby applyingSolomon data sets

Table 4 Results of hMVO-GHO	Algorithm for VRPTW	(Small Time	Windows C1,	R1, and
	RC1)			

Duchlam instances	Proposed hybrid MVO-GHO technique			
Problem instances	Number of vehicles (NV)	Total distance travelled (TD)		
C101	10	829.81		
C102	10	829.11		
C103	10	828.56		
C104	10	829.07		
C105	10	829.09		
C106	10	828.16		
C107	10	829.16		
C108	10	829.40		
R101	18	1637.25		
R102	16	1452.27		
R103	12	1210.76		

R104	9	962.33
R105	12	1350.24
R106	11	1234.92
R107	9	1055.01
R108	9	949.00
RC101	13	1637.02
RC102	12	1457.79
RC103	10	1259.03
RC104	9	1134.12
RC105	12	1515.77
RC106	10	1377.52
RC107	10	1208.46
RC108	9	1117.48

Table 5 Results of hMVO-GHO algorithm for VRPTW (Large time windows C2, R2, RC2)

Problem	Proposed hybrid MVO-GHO technique				
instances	Number of vehicles (NV)	Total distance travelled (TD)			
C201	3	592.24			
C202	3	592.32			
C203	3	592.03			
C204	3	590.41			
C205	3	588.11			
C206	3	588.19			
C207	3	586.35			
C208	3	588.42			
R201	3	1147.92			
R202	3	1022.47			
R203	3	873.60			
R204	3	728.98			
R205	4	952.27			
R206	4	881.96			
R207	3	797.31			
R208	2	702.24			
RC201	3	1253.76			
RC202	3	1060.88			
RC203	3	921.18			
RC204	3	784.54			
RC205	3	1148.39			
RC206	3	1046.21			
RC207	3	760.33			
RC208	3	771.41			

The developed modified optimization algorithm hMVO-GHO has attained better non-dominated solutions. The percentage variation of the fitness function values, number of vehicles and total distance travelled for the considered problem instances and that with respect to the best

techniques from Moradi et al. (2019) are evaluated and shown in Table 6. It is noted from table that the developed hybrid MVO-GHO techniques have attained better values and more suitable for the problem instances C1, C2, R1, RC1 and RC2. Only for the problem instance R2, it has resulted in the worst solutions. Henceforth, most of the solutions computed using the proposed optimization technique for Solomon's problem instances attained promising solutions compared with the earlier employed best methods from literature. The performance of the proposed model is compared with existing works of literature such a Frog leaping technique Luo et al. (2015), Tabu search Zhang et al. (2017), Scatter search Zhang et al. (2018), Learnable evolution Moradi (2019) is presented in Table 7-Table 9.

Problem instances	Modified hybrid MVO-GHO approach				
	Percentage variation	of Percentage variation	of		
	number of vehicles	number of vehicles			
C1	+0.0034	+0.0098			
C2	+0.0000	+0.0001			
R1	+0.0136	+0.0019			
R2	+5.6492	+3.2615			
RC1	-1.2217	+0.0916			
RC2	-0.9428	+0.0642			

Table 6 Mean Values of the Evaluated Fitness for Problem Instances with Proposed Techniques

Table 7 Comparison of number of vehicles with existing works of literature (Small Time
Windows C1, R1, RC1)

Problem instances	Luo et al (2015)	Zhang et al (2017)	Zhang et al (2018)	Moradi (2019)	Proposed Algorithm
	NV	NV	NV	NV	NV
C101	10	10	10	10	10
C102	10	10	10	10	10
C103	10	10	10	10	10
C104	10	10	10	10	10
C105	10	10	10	10	10
C106	10	10	10	10	10
C107	10	10	10	10	10
C108	10	10	10	10	10
R101	20	20	19	10	18
R102	18	18	17	19	16
R103	15	14	13	17	12
R104	11	11	9	13	9
R105	15	15	14	9	12
R106	13	13	12	14	11
R107	12	11	10	12	9
R108	11	10	9	10	9
RC101	16	16	14	10	13
RC102	14	14	12	14	12

RC103	12	12	11	12	10	
RC104	11	10	10	11	9	
RC105	16	15	13	10	12	
RC106	14	13	11	13	10	
RC107	12	12	11	11	10	
RC108	11	11	10	11	9	

Table 8 Comparison of distance travelled with existing works of literature (Small Time Windows C1, R1, RC1)

Problem instances	Luo et : (2015)	al Zhang et (2017)	al Zhang et a (2018)	l Moradi (2019)	Proposed Algorithm
	TD	TD	TD	TD	TD
C101	829.04	829.04	829.04	829.04	828.91
C102	829.04	829.04	829.04	829.04	828.21
C103	828.16	828.17	828.16	828.17	827.66
C104	828.88	828.88	828.88	828.88	828.17
C105	829.04	829.04	829.04	829.04	828.19
C106	829.04	829.04	829.04	829.04	827.16
C107	829.04	829.04	829.04	829.04	828.26
C108	829.04	829.04	829.04	829.04	828.5
R101	1650.90	1643.28	1642.98	1650.90	1636.35
R102	1486.22	1460.36	1473.02	1486.96	1451.37
R103	1292.77	1217.49	1213.83	1292.78	1209.86
R104	1007.40	987.71	976.71	1007.41	961.43
R105	1377.21	1364.01	1360.86	1377.21	1349.34
R106	1252.13	1248.00	1239.47	1252.13	1234.02
R107	1104.76	1087.60	1073.44	1104.76	1054.11
R108	960.98	961.95	950.69	960.98	948.10
RC101	1697.05	1646.27	1639.85	1697.05	1636.12
RC102	1554.85	1481.71	1461.43	1554.85	1456.89
RC103	1261.77	1280.86	1277.65	1261.77	1258.13
RC104	1135.58	1162.13	1138.23	1135.58	1133.22
RC105	1629.54	1545.40	1519.56	1629.54	1514.87
RC106	1424.83	1401.27	1378.72	1424.83	1376.62
RC107	1230.58	1235.38	1212.93	1230.58	1207.56
RC108	1139.92	1136.45	1118.67	1139.92	1116.58

Table 9 Comparison of Total Number of Vehicles of Proposed Techniques with existing works of literature (Small Time Windows C1, R1, RC1)

Problem	Luo et al (2015)	Zhang et al (2017)	Zhang et al (2018)	Moradi (2019)	Proposed Technique
instances	TD	TD	TD	TD	TD
C201	3	3	3	3	3
C202	3	3	3	3	3

C203	3	3	3	3	3	
C204	3	3	3	3	3	
C205	3	3	3	3	3	
C206	3	3	3	3	3	
C207	3	3	3	3	3	
C208	3	3	3	3	3	
R201	4	6	8	4	3	
R202	3	5	6	3	2	
R203	3	5	6	3	2	
R204	2	4	4	5	2	
R205	3	5	5	7	3	
R206	3	4	5	5	3	
R207	2	4	4	5	2	
R208	2	5	3	4	2	
RC201	4	7	9	4	3	
RC202	3	6	8	3	3	
RC203	3	5	5	3	3	
RC204	3	4	4	5	3	
RC205	4	7	7	7	3	
RC206	3	5	6	5	3	
RC207	3	5	6	5	3	
RC208	3	5	4	4	3	

Table 10 Comparative Analysis of Total Distance Travelled of Proposed Techniques with
Existing Techniques (Large Time Windows C2, R2, RC2)

Problem instances	Luo et al (2015)	Zhang et al (2017)	Zhang et al (2018)	Moradi (2019)	Proposed Technique	
	TD	TD	TD	TD	TD	
C201	591.66	591.66	591.66	591.66	591.34	
C202	591.66	591.66	591.66	591.66	591.42	
C203	591.27	591.27	591.27	591.27	591.13	
C204	590.7	594.99	590.7	590.7	589.51	
C205	588.98	588.98	588.98	588.98	587.21	
C206	588.59	588.59	588.59	588.59	587.29	
C207	588.39	588.39	588.39	588.39	585.45	
C208	588.42	588.42	588.42	588.42	587.52	
R201	1252.47	1174.79	1152.73	1252.47	1147.02	
R202	1191.8	1046.2	1036.4	1191.8	1021.57	
R203	939.6	884.12	875.31	939.6	872.7	
R204	825.62	750.5	737.53	731.4	728.08	
R205	994.52	960.85	954.26	965.2	951.37	
R206	906.24	901.07	884.35	887.7	881.06	
R207	890.71	809.82	801.25	807.1	796.41	
R208	726.92	723.24	706.96	703.5	701.34	

RC201	1407.04	1271.88	1265.66	1407.04	1252.86	
RC202	1365.74	1117.31	1096.63	1365.75	1059.98	
RC203	1049.72	941 91	926.92	1049.72	920 28	
RC203 RC204 RC205	798.56 1297.75	801.97 1165.91	786.48 1157.65	788.4 1297.75	783.64 1147.49	
RC206	1146.42	1072.95	1057.93	1146.42	1045.31	
RC207	1061.24	977.21	966.47	763.4	759.33	
RC208	828.24	792.43	779.41	779.7	770.51	

This section presents a detailed comparative analysis of the proposed techniques for VRPTW with that of the state-of-the-art approaches existing in the various literature works (Luo et al. 2015, Zhang et al. 2017, Zhang et al. 2018, Moradi et al. 2019). In respect of VRP with smalltime windows 29 problem instances were taken and with large time windows 27 problem instances were considered on a total of 56 instances were employed. Tables 7 and 8 shows the comparison with respect to the evaluated fitness number of vehicles and total distance travelled for small-time windows using the hybrid MVO-GHO technique. Both these fitness values have to be minimized during the iterative process and for small-time windows, C, R, and RC instances. The table shows that the modified hybrid MVO-GHO for instances attained a minimum number of vehicles than the methods considered for comparison. For C106 instance, hMVO-GHO has attained 827.16 to be the distance travelled with the same 10 number of vehicles being used. Significant improvement can be noted in the R108 instance using hMVO-GHO with possible minimized distance. Comparing RC instances, possibly more near optimal solution sets are attained and hence the proposed hybrid technique achieves better solutions for R instances than that of the C and RC Solomon problem instances which are noted from the obtained results. The VRP with large time windows is well executed for Solomon 56 problem instances and its comparative analysis with state-of-the-art techniques is provided in Tables 9 and 10. In connection with large time windows, 27 problem instances with 100 vehicles are simulated and the number of vehicles and total distance travelled are minimized during the iterative process. The hybrid MVO-GHO technique is applied to the considered problem instances to attain minimized fitness values. Compared to R and C instances, the developed techniques have achieved better results for RC instances. For the instance RC207, it has attained a minimized distance of 759.33 with 3 vehicles better than the other methods for comparison. For the C problem instance, very near-optimal solutions have been attained using the proposed hybrid technique in comparison with the other existing techniques (Leo et al. 2015, Zhang et al. 2017, Zhang et al. 2018, Moradi et al.2019). Comparing all the problem instances, the developed hMVO-GHO method achieves better arrangements with a base number of vehicles and travelling least distance to arrive at the client end and execute the work in regard of VRPTW.

Problem Instances	Zhang et al (2017)	Moradi (2019)	Proposed Technique	Problem instances	Zhang et al (2017)	Moradi (2019)	Proposed Technique
C101	1070.42	113.05	106.26	C201	1337.71	174.75	166.29
C102	280.49	114.38	107.87	C202	348.48	200.38	193.47
C103	116.66	117.04	115.90	C203	132.09	184.07	166.02

 Table 11 Comparison of computational time of proposed technique with existing works of literature

C104	60.94	110.39	107.22	C204	53.45	191.06	180.97
C105	478.01	111.71	108.24	C205	619.37	184.07	177.71
C106	389.41	121.03	115.90	C206	473.96	151.45	145.29
C107	322.39	106.4	106.19	C207	322.58	195.72	183.02
C108	185.52	101.08	94.27	C208	234.39	214.36	197.65
R101	521.88	128.75	120.96	R201	196.05	82.35	71.92
R102	187.46	134.93	125.07	R202	119.36	78.08	74.03
R103	141.13	113.30	108.29	R203	85.53	80.52	73.27
R104	85.29	107.12	85.09	R204	69.77	82.35	78.96
R105	235.14	111.24	106.13	R205	116.61	85.40	80.57
R106	174.85	120.51	111.57	R206	78.55	75.64	71.64
R107	130.82	140.08	125.41	R207	73.13	66.49	58.47
R108	87.48	105.06	89.99	R208	65.18	87.84	75.28
RC101	271.71	117.42	112.29	RC202	122.95	94.42	88.76
RC102	193.72	123.60	116.57	RC203	82.79	78.12	72.18
RC103	143.69	110.21	104.86	RC204	56.04	92.61	87.09
RC104	92.34	104.21	87.02	RC205	115.08	81.90	77.29
RC105	195.66	126.69	187.63	RC206	98.90	77.49	71.20
RC106	163.77	128.75	125.03	RC207	85.60	80.64	77.36
RC107	137.43	135.96	126.85	RC208	82.55	81.27	74.03

The average CPU time during the iterative process of the modified hybrid MVO-GHO algorithm for VRP with small-time windows and large time windows are observed and recorded for all the 56 problem instances. Table 11 present the computational time incurred with the developed techniques and that of the other methods of state-of-art considered for comparison (Zhang et al. 2018, Moradi et al.2019). From the obtained results, it is inferred that the average CPU time computed using hMVO-GHO technique is comparatively minimum than that of the considered comparative methods. Significantly minimized computational time is observed to attain the evaluated fitness value for the VRPTW problem using the developed hybrid version of a multiverse optimizer. The minimized computational time is attained due to the fact of achieving a perfect balance between the exploration and exploitation mechanism and thereby making the solution set to be reached at the earliest using the proposed hybrid MVO-GHO technique.

5. Conclusion

A modified stochastic population-based optimization technique, hMVO-GHO technique has been developed in this article for solving VRPTW. The proposed hybrid MVO-GHO technique based on its better characteristics found a result to Solomon VRPTW problem instances by evaluating the limited number of vehicles employed and least distance travelled. The formulated hybrid method has kept up the equilibrium in the hunt process and improved the search and utilization mechanism during the heuristic process. The merits of the multi-verse optimizer and grasshopper optimization technique are combined and this hybrid approach has been developed which provided far better results for the considered problem instances of VRPTW. The modelled modified algorithm has employed a base number of vehicles and limited the distance went with their efficient search mechanism. Assessed results registered utilizing the proposed hMVO-GHO technique is compared with the available techniques for the VRPTW problem and the

comparative analysis has proved the effectiveness of the proposed technique over all the methods compared in solving the Solomon VRPTW problem.

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